

# Phase Modulation in APT Spectra for ABX Patterns

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Anomalous APT spectra are reported for an organophosphorus compound containing methylene  $^{13}\text{C}$  nuclei coupled to two  $^{31}\text{P}$  nuclei. Strong coupling effects in these ABX spin systems are shown to account for the anomalous phases and intensities of the APT spectra by density matrix simulations. © 1997 by John Wiley & Sons, Ltd.

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## INTRODUCTION

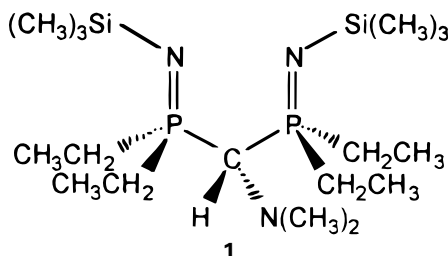
APT,<sup>1</sup> a  $^{13}\text{C}$  spin-echo pulse sequence<sup>2</sup> with the  $^1\text{H}$  decoupler gated off during the delay period between the excitation and refocusing pulses, is used routinely in  $^{13}\text{C}$  NMR spectroscopy to determine  $^{13}\text{C}$  resonance multiplicities. Generally the APT spectrum is obtained with the delay equal to  $1/J_{\text{CH}}$ , where  $J_{\text{CH}}$  is the one-bond proton–carbon coupling constant. This gives  $^{13}\text{C}$  spectra in which resonances from quaternary and methylene carbons are  $180^\circ$  out of phase from those originating from methine and methyl carbons. False multiplicity assignments are possible in  $^{13}\text{C}$  dilabelled compounds because of  $J$  modulation of the  $^{13}\text{C}$  resonances caused by homonuclear coupling during the spin-echo pulse sequence<sup>3</sup> or when the compound contains  $\text{CH}_n$  groups with very large  $J_{\text{CH}}$  values.<sup>4</sup> In this paper we report observations of phase modulation in APT spectra caused by strong coupling effects.

## RESULTS AND DISCUSSION

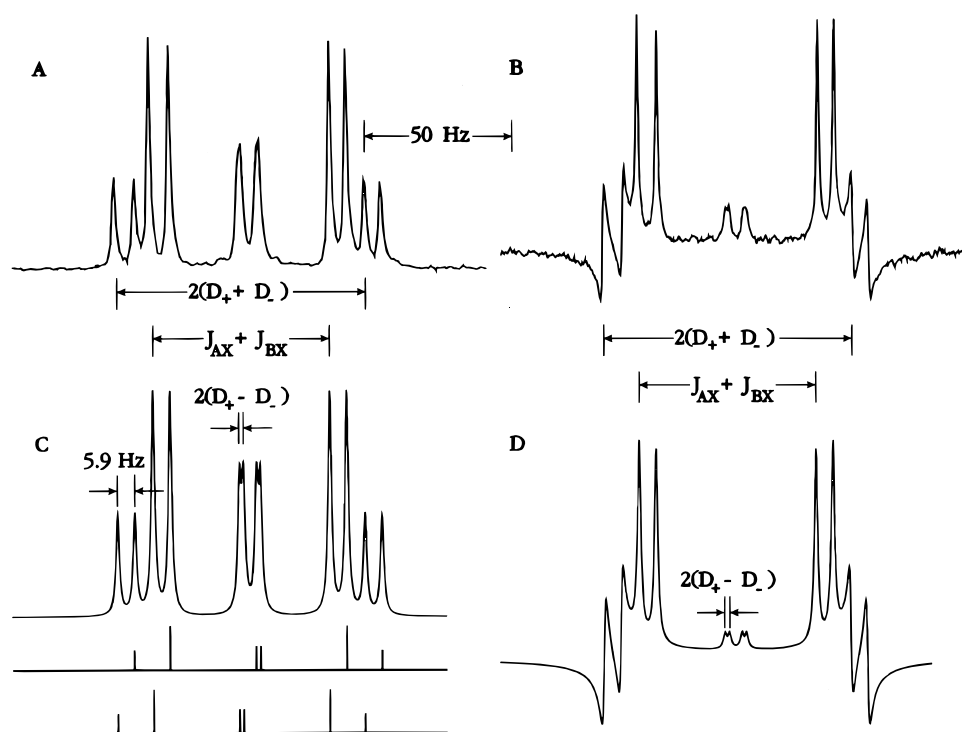
The  $^{13}\text{C}\{^1\text{H}\}$  spectra of organophosphorus molecules containing chemically equivalent phosphorus nuclei such as structure 1 (the synthesis of 1 and related molecules is described elsewhere<sup>5</sup>) often show second-order coupling patterns and such spectra can be analyzed fully.<sup>6</sup> The two pairs of chemically non-equivalent methylene carbons form the X parts of two nearly coincident ABX patterns shifted by 0.08 ppm as shown in Fig. 1(A). The quantities  $D_+$  and  $D_-$  used in Fig. 1 and the angles  $\phi_+$  and  $\phi_-$  used in Table 1 follow the definitions of Pople *et al.*<sup>7</sup> The ABX patterns arise because

the methylene carbons couple differently to the two phosphorus nuclei which are magnetically non-equivalent because the phosphorus which is directly bonded to the  $^{13}\text{C}$  nucleus experiences a small isotope shift. The ABX spectra are similar to those given in Ref. 6.

The APT spectrum of 1, obtained with a  $45-\tau_1-180-\tau_1-\tau_2-180-\tau_2$ -Acquire sequence with the  $^1\text{H}$  decoupler gated off during the  $\tau_1-180$  time interval, is shown in Fig. 1(B). The anomalous lineshapes in this APT spectrum are rather striking—the outermost lines in each of the six line patterns [at frequencies  $\nu_X \pm (D_+ + D_-)$ ] have dispersion lineshapes, the innermost pairs of lines [at frequencies  $\nu_X \pm (D_+ - D_-)$ ] have absorption lineshapes with much lower intensities than in the  $^{13}\text{C}\{^1\text{H}\}$  spectrum in Fig. 1(A), while the intense lines at frequencies  $\nu_X \pm (J_{\text{AX}} + J_{\text{BX}})/2$  have absorption lineshapes with amplitudes similar to those in the normal spectrum. The effect of strong coupling on spectral amplitudes has been reported for several spin-echo experiments,<sup>8</sup> but not for APT. The results of a density matrix analysis of the behavior of the X part of an ABX spin system when subjected to the APT pulse sequence, and to the simpler  $90-\tau_1-180-\tau_1$ -Acquire Hahn spin-echo sequence, are given in Table 1. The origin of the phase and amplitude anomalies observed in the APT spectrum is due to the mixing of magnetizations from lines at  $\nu_X \pm (D_+ + D_-)$  and  $\nu_X \pm (D_+ - D_-)$  produced by the  $180^\circ$  pulses. On the other hand, the magnetizations of the  $\nu_X \pm (J_{\text{AX}} + J_{\text{BX}})/2$  lines are not mixed



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**Figure 1.** CH<sub>2</sub> region of the 75 MHz <sup>13</sup>C{<sup>1</sup>H} and APT spectra of **1**: (A) observed <sup>13</sup>C{<sup>1</sup>H}; (B) observed APT; (C) calculated <sup>13</sup>C{<sup>1</sup>H} with 'stick' spectra below; (D) calculated APT. Calculated spectra are based on a pair of ABX patterns with identical spectral parameters ( $\nu_A - \nu_B = 1.0$  Hz,  $J_{AB} = 31.7$  Hz,  $J_{AX} = 59.0$  Hz,  $J_{BX} = 2.0$  Hz) offset by 5.9 Hz. For APT,  $\tau_1 = 0.007$  s and  $\tau_2 = 0.001$  s.

by the 180° pulses and are completely refocused during the next delay period. The simulated <sup>13</sup>C{<sup>1</sup>H} and APT spectra of **1** are shown in Fig. 1(C) and (D), respectively.

The relative magnitudes of the absorptive and dispersive components of the lines in the APT spectra at frequencies  $\nu_X \pm (D_+ + D_-)$  and  $\nu_X \pm (D_+ - D_-)$  are determined by the magnitudes of the delays  $\tau_1$  and  $\tau_2$ , and by the magnitudes of the magnetic parameters  $D_+$  and  $D_-$ . In general, the dispersive components of the inner lines at frequencies  $\nu_X \pm (D_+ - D_-)$  are very small when  $\nu_A - \nu_B$  is small as in compound **1**. The magnitudes of the absorptive components of the inner lines

vary strongly with  $D_+$ ,  $D_-$  and  $\tau_1$  provided  $D_+ \tau_1$ ,  $D_- \tau_1 > 0.1$ . The dispersive components of the outer lines at frequencies  $\nu_X \pm (D_+ + D_-)$  are also significant when  $D_+ \tau_1$ ,  $D_- \tau_1 > 0.1$ , and when the coupling constants satisfy the relationship  $0.3 |J_{AX} - J_{BX}| \lesssim J_{AB} \lesssim 0.6 |J_{AX} - J_{BX}|$ . When  $\nu_A - \nu_B \approx 0$  as in compound **1**,  $D_+ \approx D_- = D$ , and the magnitudes of the absorptive components of the inner lines are approximately proportional to  $1 - 2 \sin^2(\phi_+ - \phi_-) [1 - \cos(4\pi D \tau_1)]$ . Furthermore, the magnitudes of the dispersive components of the outer lines are approximately proportional to  $\sin(4\pi D \tau_1) [1 - \cos(4\pi D \tau_1)]$  in this limit,

**Table 1.** Amplitudes for lines in the spin-echo and APT spectra for the X part of an ABX spin system<sup>a</sup>

Spectra	Frequency	Absorption intensity	Dispersion intensity
Spin-echo	$\nu_X \pm (D_+ + D_-)$	$SA_i$	$\pm SA_r$
	$\nu_X \pm (J_{AX} + J_{BX})/2$	1	0
	$\nu_X \pm (D_+ - D_-)$	$-CB_i$	$\pm CB_r$
APT	$\nu_X \pm (D_+ - D_-)$	$S \{C^2[-A_r \sin(\Omega_+ \tau_2) + A_i \cos(\Omega_+ \tau_2)]$ $+ CS (B_r[-\sin(\omega_+ \tau_2) + \sin(\omega_- \tau_2)]$ $+ B_i[\cos(\omega_+ \tau_2) + \cos(\omega_- \tau_2)]) - S^2 A_i\}$	$\mp S \{C^2[A_r \cos(\Omega_+ \tau_2) + A_i \sin(\Omega_+ \tau_2)]$ $+ CS (B_r[\cos(\omega_+ \tau_2) - \cos(\omega_- \tau_2)]$ $+ B_i[\sin(\omega_+ \tau_2) + \sin(\omega_- \tau_2)]) + S^2 A_r\}$
	$\nu_X \pm (J_{AX} + J_{BX})/2$	1	0
	$\nu_X \pm (D_+ + D_-)$	$C \{S^2[B_r \sin(\Omega_- \tau_2) - B_i \cos(\Omega_- \tau_2)]$ $+ CS (A_r[\sin(\omega_+ \tau_2) + \sin(\omega_- \tau_2)]$ $- A_i[\cos(\omega_+ \tau_2) + \cos(\omega_- \tau_2)]) + C^2 B_i\}$	$\pm C \{S^2[B_r \cos(\Omega_- \tau_2) + B_i \sin(\Omega_- \tau_2)]$ $+ CS (A_r[\cos(\omega_+ \tau_2) - \cos(\omega_- \tau_2)]$ $+ A_i[\sin(\omega_+ \tau_2) - \sin(\omega_- \tau_2)]) + C^2 B_r\}$

$$^a D_{\pm} = \frac{1}{2} \sqrt{[\nu_A - \nu_B \pm (J_{AX} - J_{BX})/2]^2 + J_{AB}^2};$$

$$C = \cos(\phi_+ - \phi_-);$$

$$S = \sin(\phi_+ - \phi_-);$$

$$\omega_{\pm} = 4\pi D_{\pm};$$

$$\Omega_{\pm} = \omega_{\pm} \pm \omega_-;$$

$$A_r = SC^2[\sin(\omega_+ \tau_1) + \sin(\omega_- \tau_1) - \sin(\Omega_+ \tau_1)];$$

$$A_i = S\{1 + C^2[-1 + \cos(\omega_+ \tau_1) + \cos(\omega_- \tau_1) - \cos(\Omega_+ \tau_1)]\};$$

$$B_r = CS^2[-\sin(\omega_+ \tau_1) + \sin(\omega_- \tau_1) + \sin(\Omega_- \tau_1)];$$

$$B_i = -C\{1 + S^2[-1 + \cos(\omega_+ \tau_1) + \cos(\omega_- \tau_1) - \cos(\Omega_- \tau_1)]\}.$$

so the APT lineshapes are very sensitive to the value of  $\tau_1$  and to the values of  $J_{AB}$  and  $|J_{AX} - J_{BX}|$  which define the parameter  $D$ . The APT lineshapes are much more sensitive to the values of the magnetic parameters than the standard  $^{13}\text{C}\{^1\text{H}\}$  spectra are, so APT and/or spin-echo spectra may be used to refine estimates of

magnetic parameters obtained from analysis of  $^{13}\text{C}\{^1\text{H}\}$  spectra. INEPT<sup>9</sup> and DEPT<sup>10</sup> spectra of **1** show very little phase distortion because the delay periods in these sequences are much shorter than the long delay period  $\tau_1$  used in APT.

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